



TP B.6

CB table lengths of travel for different speeds, accounting for rail rebound and drag losses

supporting:

“The Illustrated Principles of Pool and Billiards”

<http://billiards.colostate.edu>

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Typical speeds for a range of shots:

$$\begin{aligned}
 v_{\text{touch}} &:= 1.5 \cdot \text{mph} & v_{\text{slow}} &:= 3 \cdot \text{mph} & v_{\text{medium_soft}} &:= 5 \cdot \text{mph} & v_{\text{medium}} &:= 7 \cdot \text{mph} \\
 v_{\text{medium_fast}} &:= 8 \cdot \text{mph} & v_{\text{fast}} &:= 12 \cdot \text{mph} & v_{\text{power}} &:= 20 \cdot \text{mph}
 \end{aligned}$$

Relevant physical properties:

$$\begin{aligned}
 \mu_s &:= 0.2 & \text{typical ball-cloth coefficient of sliding friction} \\
 \mu_r &:= 0.01 & \text{typical ball-cloth coefficient of rolling resistance}
 \end{aligned}$$

From TP 4.1, the distance required for a rolling ball to stop is:

$$d_{\text{roll_stop}}(v) := \frac{v^2}{2 \cdot \mu_r \cdot g}$$

Table lengths vs. speed, accounting for rail rebound and drag losses:

$$e_c := 0.7 \quad \text{typical ball/rail COR with ball rolling into the rail cushion (see HSV B.15)}$$

When the CB rebounds off a rail cushion, speed is lost. If we assume the CB rebounds off the rail with stun (see HSV B.15 - a rolling ball usually rebounds with stun), the resulting skid distance and speed change are (from TP 4.1):

$$d_{\text{skid}}(v) := \frac{12 \cdot v^2}{49 \cdot \mu_s \cdot g}$$

$$v_{\text{skid}}(v, x) := \sqrt{v^2 - 2 \cdot \mu_s \cdot g \cdot x}$$

$$v_{\text{skid}}(v, d_{\text{skid}}(v)) = \frac{5}{7} \cdot v$$

In the analysis below, to keep things reasonably simple, we assume the CB always rebounds off the rail with stun. HSV B.15 shows that a skidding ball usually rebounds with some roll, but the overall rebound efficiency, taking post-rebound skid into consideration, is fairly consistent for most shots.

While the CB rolls, it slowly loses speed due to rolling resistance over distance x :

$$\frac{1}{2} \cdot m \cdot v'^2 = \frac{1}{2} \cdot m \cdot v^2 - \mu_r \cdot m \cdot g \cdot x$$

so the function of speed over distance, during rolling, is:

$$v_{\text{roll}}(v, x) := \sqrt{v^2 - 2 \cdot \mu_r \cdot g \cdot x}$$

Determine CB travel distance for a rolling CB with rail collisions:

TL := 100·in TL = 8.333·ft 9' table playing length

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d(v) :=
  x ← 0
  v ← v
  n ← 0
  roll ← 1
  if (d_roll_stop(v) < TL)
    "less than one table length"
    x ← d_roll_stop(v)
  otherwise
    "ball will roll into a rail"
    while (v > 0)
      if (roll = 1)
        if d_roll_stop(v) < (n + 1)TL - x
          "won't make it to rail again"
          x ← x + d_roll_stop(v)
          break
        otherwise
          "roll to the rail"
          n ← n + 1
          v ← v_roll(v, n·TL - x)
          x ← n·TL
          "rebound off the rail"
          v ← e_c·v
          roll ← 0

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| | | | otherwise
| | | | "(roll = 0) : ball skidding"
| | | | if (dskid(v) < TL)
| | | | | "ball will roll before next rail"
| | | | | x ← x + dskid(v)
| | | | | v ←  $\frac{5}{7} \cdot v$ 
| | | | | roll ← 1
| | | | otherwise
| | | | | "ball will skid into next rail"
| | | | | n ← n + 1
| | | | | v ← vskid(v, TL)
| | | | | x ← n · TL
| | | | | "rebound off the rail"
| | | | | v ← ec · v
| | | | | roll ← 0
| | | |
| | |
| |
|
x

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$$d(v_{\text{touch}}) = 7.522 \cdot \text{ft}$$

$$d(v_{\text{slow}}) = 14.033 \cdot \text{ft}$$

$$d(v_{\text{medium}}) = 25.041 \cdot \text{ft}$$

$$d(v_{\text{fast}}) = 30.752 \cdot \text{ft}$$

$$d(v_{\text{power}}) = 39.291 \cdot \text{ft}$$

table lengths of travel:

$$\frac{d(v_{\text{touch}})}{\text{TL}} = 0.903$$

$$\frac{d(v_{\text{slow}})}{\text{TL}} = 1.684$$

$$\frac{d(v_{\text{medium}})}{\text{TL}} = 3.005$$

$$\frac{d(v_{\text{fast}})}{\text{TL}} = 3.69$$

$$\frac{d(v_{\text{power}})}{\text{TL}} = 4.715$$

rolling lag shot: $v := v_{\text{slow}} = 3 \cdot \text{mph}$ (estimate)

Given

$$d(v) = 2 \cdot \text{TL}$$

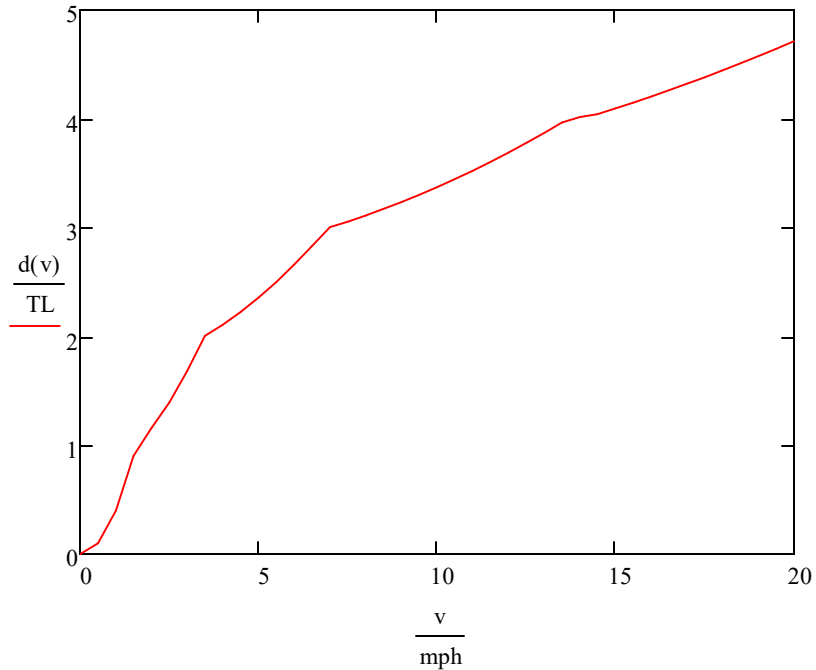
$$v_{\text{lag}} := \text{Find}(v)$$

$$v_{\text{lag}} = 3.465 \cdot \text{mph}$$

$$\frac{d(v_{\text{lag}})}{\text{TL}} = 2$$

$v := 0 \cdot \text{mph}, 0.5 \cdot \text{mph}.. v_{\text{power}}$

$v_{\text{power}} = 20 \cdot \text{mph}$



$$\frac{v_{\text{fast}}}{v_{\text{medium}}} = 1.714$$

$$\frac{d(v_{\text{fast}})}{d(v_{\text{medium}})} = 1.228$$

$$\frac{v_{\text{fast}}}{v_{\text{slow}}} = 4$$

$$\frac{d(v_{\text{fast}})}{d(v_{\text{slow}})} = 2.191$$

$$\frac{v_{\text{power}}}{v_{\text{touch}}} = 13.333$$

$$\frac{d(v_{\text{power}})}{d(v_{\text{touch}})} = 5.224$$

So the speed must be increased by a much larger percentage to create a given percentage of distance increase, and this effect is even stronger at faster speeds and longer distances. In other words, it takes a lot more speed to create more distance, especially at higher speeds and longer distances.